



Active Water-Wave Absorber

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ME236: Control & Optimization of Distributed
Parameters

Professor Alex Bayen

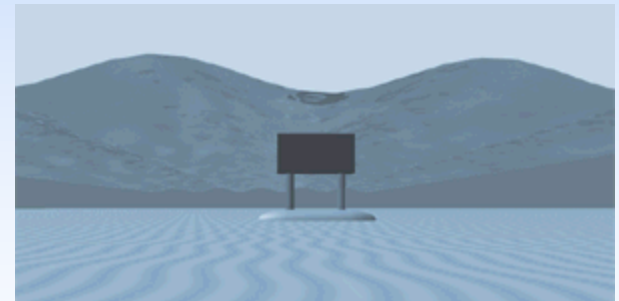
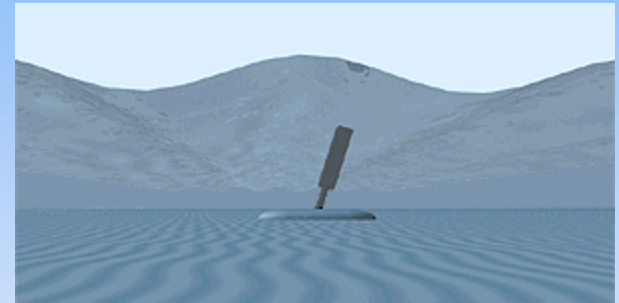
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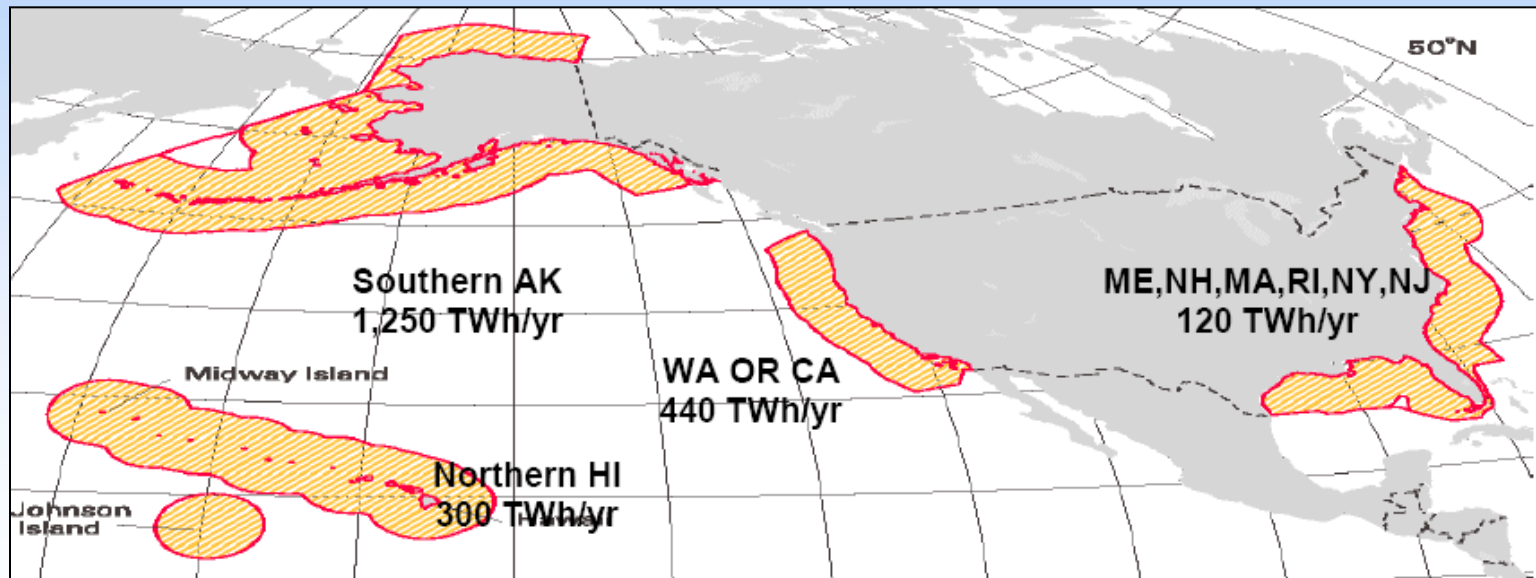


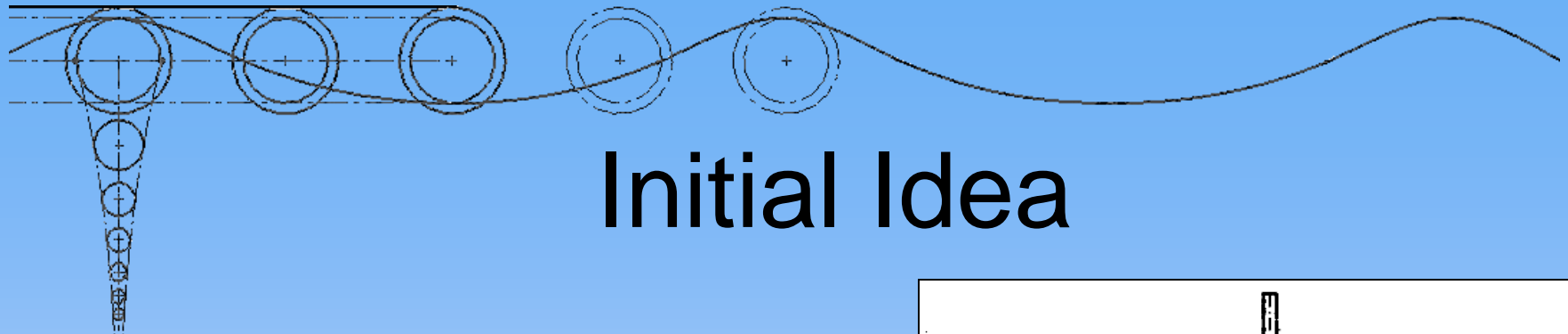
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Motivation

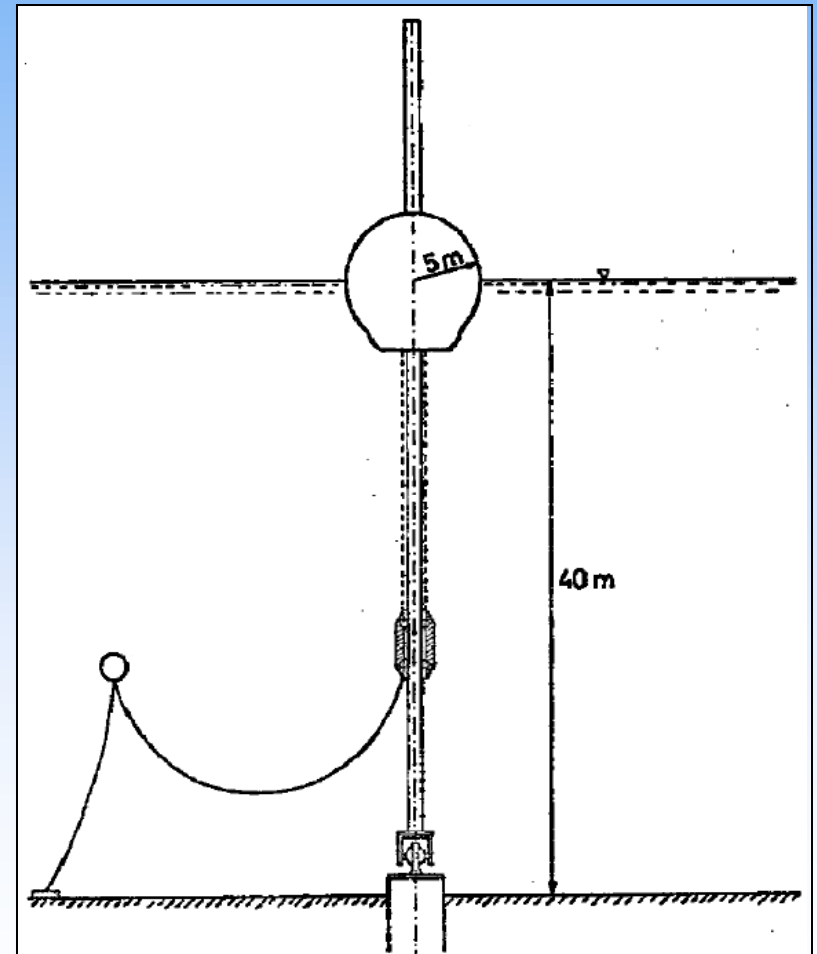
- Significant amounts of energy is stored in the ocean
- Large potential for extracting energy from waves
- Control is the key to optimizing energy extraction and economic feasibility.





Initial Idea

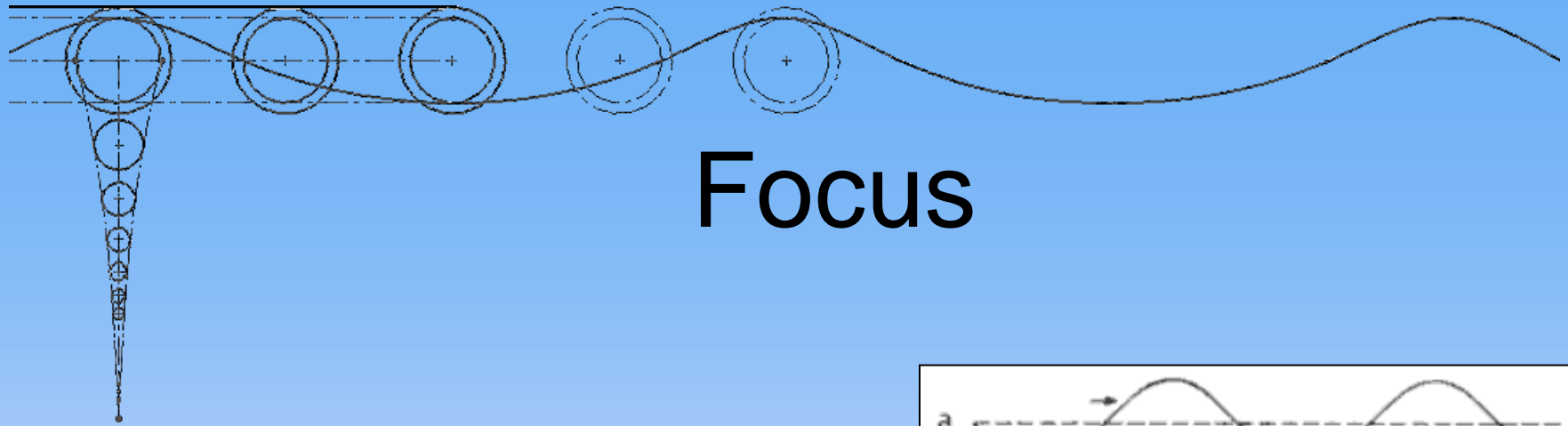
- 1-Degree of Freedom Point Absorber
- Direct Drive Linear Generator
- Optimize Hydrodynamic Parameters
 - Added Mass
 - Added Damping
- Optimize Phase Control





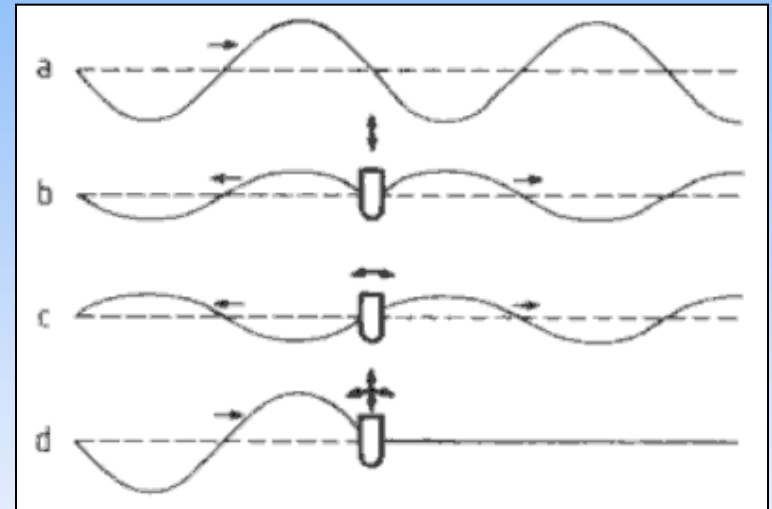
Literature Search

- Eriksson, M., Isber, J., Leijon, M. “Hydrodynamic Modeling of a Direct-Drive Wave Energy Converter.” *International Journal of Engineering Science*, vol. 43, pages 1377-1387, 2005.
- *Falnes, Johannes “Ocean Waves and Oscillating Systems: Linear Interactions Including Wave-energy Extraction.” Cambridge University Press, Cambridge. 2002.*
- Havelock, T. H., “Forced Surface-Waves on Water.” *Philosophic Magazine of Science*, vol. 8, no. 51, Oct. 1929.
- **Milgram, Jerome H., “Active Water-Wave Absorbers.” *Journal Fluid Mechanics*, vol. 43, part 4, pages 845-859, 1970.**
- Yeung, Ronald W. “Added Mass and Damping of a Vertical Cylinder in Finite-depth Waters.” *Applied Ocean Research*, vol. 3, no. 3, pages 119-133. 1981.

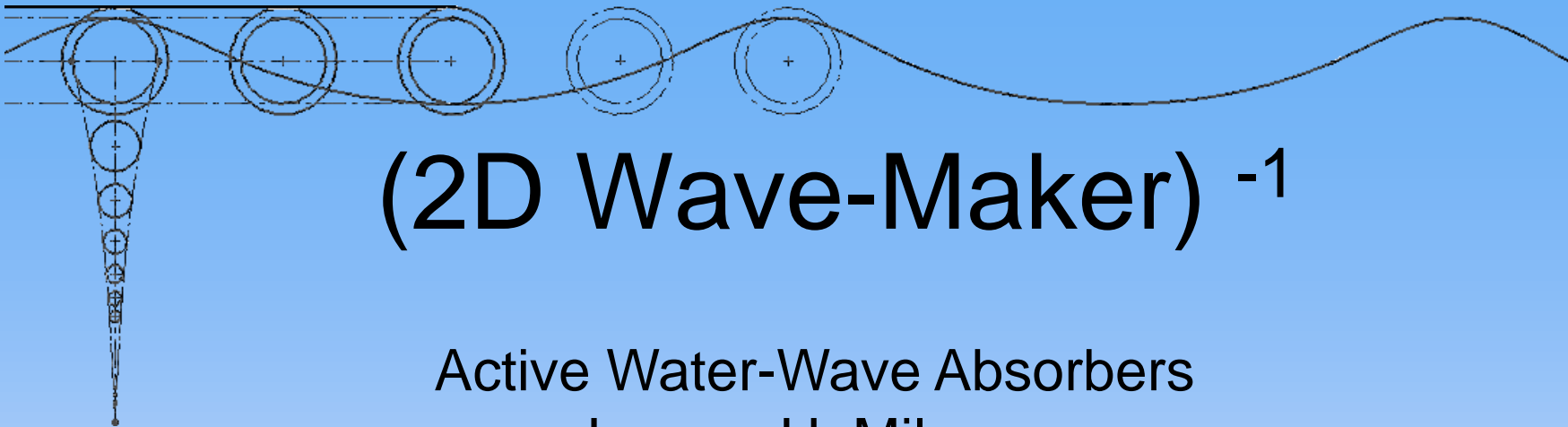


Focus

- Simplify the Problem!



- *“To absorb a wave means to generate a wave or, in other words: To destroy a wave is to create a wave.” – Johannes Falnes*

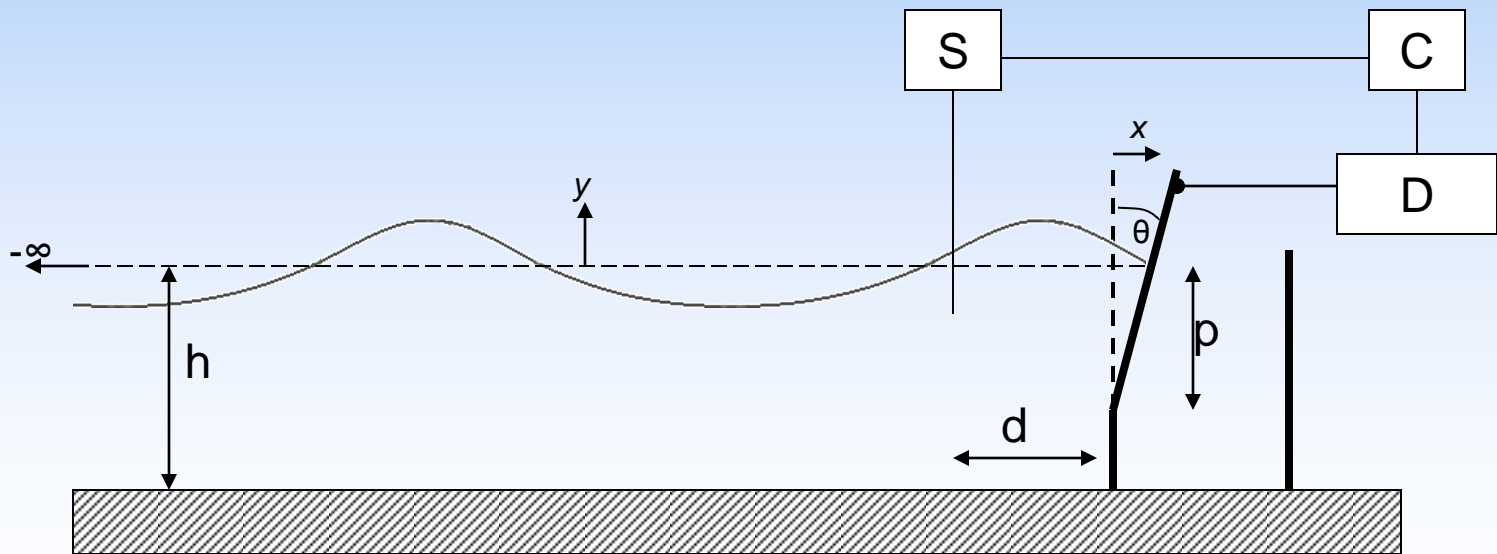


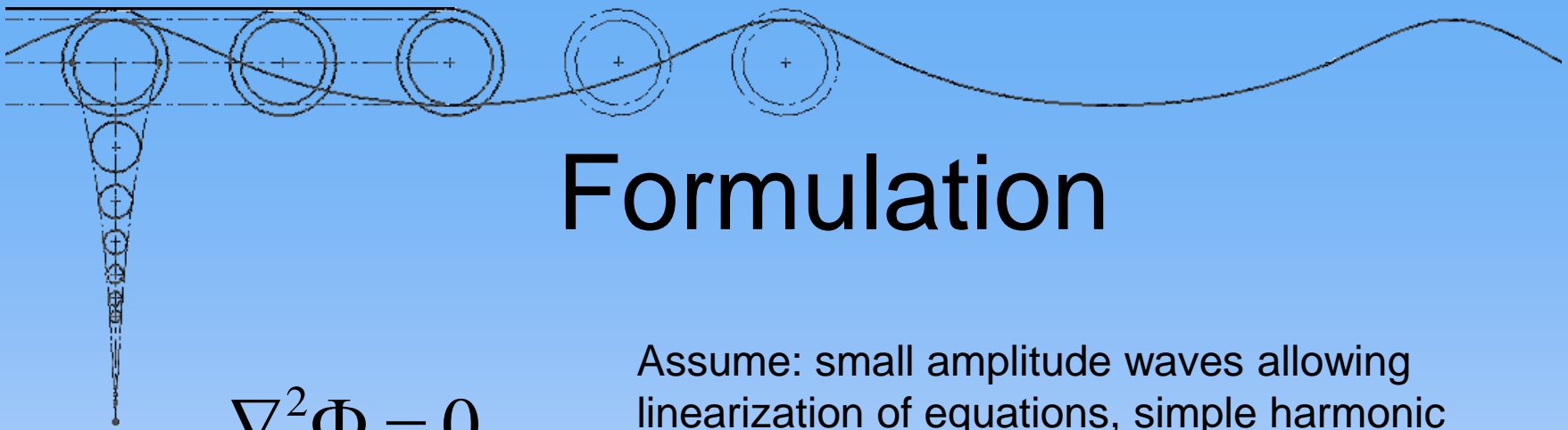
(2D Wave-Maker) ⁻¹

Active Water-Wave Absorbers

Jerome H. Milgram

Journal of Fluid Mechanics (1970), vol. 43, pp. 845-859





Formulation

Assume: small amplitude waves allowing linearization of equations, simple harmonic oscillations, initially irrotational fluid, neglect viscosity and surface tension.

$$\nabla^2 \Phi = 0$$

Boundary Conditions

$$\Phi_{tt} + g\Phi_y = 0$$

on $y = 0$

- Dynamic free surface

$$\Phi_y = N_t$$

on $y = 0$

- Kinematic free surface

$$\Phi_y = 0$$

on $y = -h$

- Impermeable floor

$$\Phi_x = \Psi_t$$

on $x = 0$

- Termination (Flapper) wall

$$|\nabla \Phi| < \infty$$

at $x = -\infty$

- Condition at infinity



Derivations

- Separation of Variables used to solve Laplacian

$$\Phi = \Phi(x, y, t) = \sum_{k=-\infty}^{\infty} C_k F_k(x) G_k(y) e^{-i\lambda t}$$

$$F_k(x) = e^{if_k x}$$

$$G_k(y) = \cosh f_k(y + h)$$

- Free Surface BC leads to the dispersion relation

$$\frac{\lambda^2 h}{f h} = g \tanh(fh)$$



Calculations

- Due to boundedness of the boundary condition at negative infinity the potential function leads to

$$\Phi(x, y) = A_0' \cosh f_0(y+h)e^{-if_0x} + \sum_{n=0}^{\infty} A_n \cosh f_n(y+h)e^{if_nx}$$

where, the A_0' term refers to the wave reflected from the flapper wall.

- Channel termination (Flapper - active absorber)

where, $\Psi(y, t) = B\psi(y)e^{-i\lambda t}$

$$\psi(y) = \begin{cases} y + p & y \geq -p \\ 0 & y < -p \end{cases}$$

- The channel termination boundary condition then requires the following:

$$\Phi_x = \Psi_t$$

$$(A_0 - A_0') \cosh f_0(y+h) + \sum_{n=1}^{\infty} A_n f_n \cosh f_n(y+h) = -B\lambda\psi(y)$$



Orthogonality

- The condition of orthogonality must be satisfied at the moving termination.

$$\int_{-h}^0 G_k(y)G_n(y)dy = 0 \quad \text{for} \quad k \neq n$$

- This condition applies to the results of the previous page and allows the definition of the following integrals,

$$I_n^{(1)} = \int_{-h}^0 \cosh^2 f_n(y+h)dy = \frac{1}{2}h \left[1 + \frac{1}{2f_n h} \sinh 2f_n h \right]$$

$$I_n^{(2)} = \int_{-h}^0 \psi(y) \cosh f_n(y+h)dy = \frac{p}{f_n} \sinh f_n h + \frac{1}{f_n^2} [\cosh f_n(h-p) - \cosh f_n h]$$

- These integrals can then be used to define the ratio of coefficient values

$$\left. \begin{array}{l} \text{for } n = 0, \quad A_0 - A_0' \\ \text{for } n \neq 0, \quad A_n \end{array} \right\} = -\frac{\lambda}{f_n} B \frac{I_n^{(2)}}{I_n^{(1)}}$$



Complete Absorption

- For complete absorption the term $A'_0 = 0$. So we can use the ratio from the previous page to define the complex coefficient of motion, B .

$$B = \frac{-A_0 f_0^2 [2f_0 h + \sinh 2f_0 h]}{4\lambda \{f_0 p \sinh f_0 h + \cosh f_0 (h - p) - \cosh f_0 h\}}$$

- Surface elevation can be calculated using the velocity potential and the kinematic free surface condition.

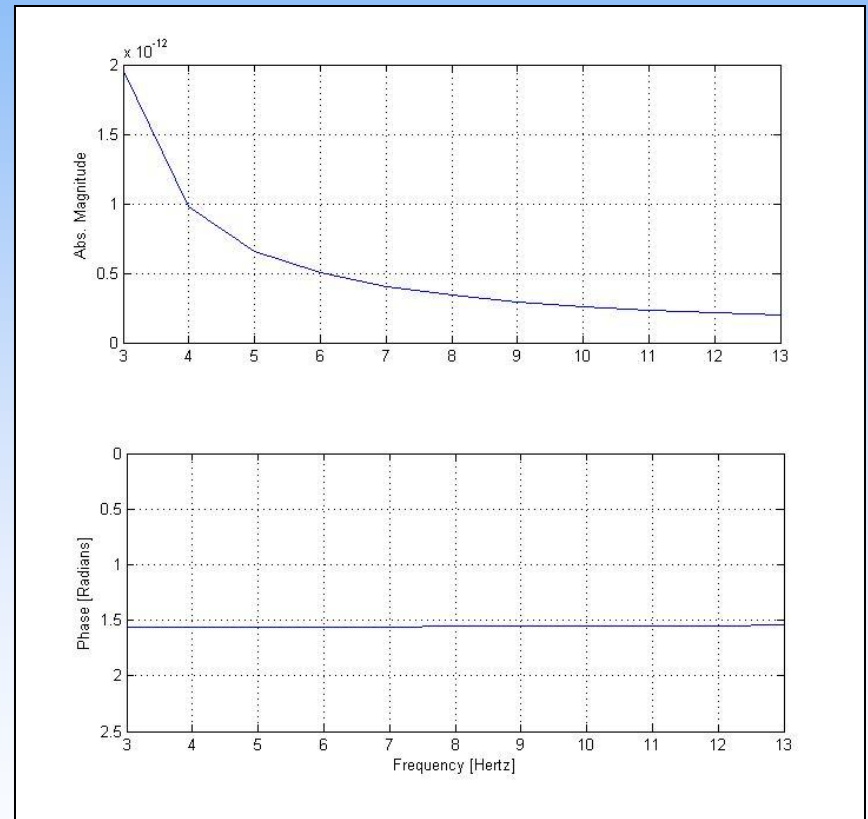
$$\eta(x) = \frac{-1}{i\lambda} f_0 (A_0 e^{-if_0 x} + A_0 e^{if_0 x}) \sinh f_0 h - \frac{1}{i\lambda} \sum_{n=1}^{\infty} f_n A_n \sinh f_n h e^{if_n x}$$

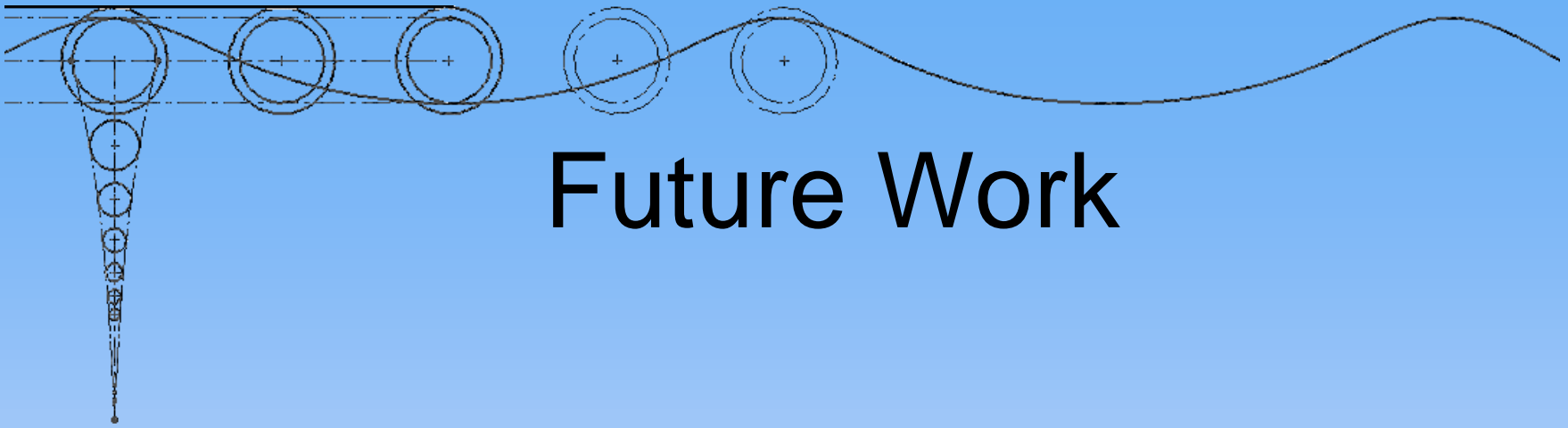
Transfer Function

- Frequency dependent ratio of complex termination motion to surface elevation at the location of the sensor $x = -d$.

$$H_a(\lambda) = \frac{i}{\sum_{n=0}^{\infty} \frac{I_n^{(2)}}{I_n^{(1)}} \sinh(f_n h) e^{-if_n d}}$$

- Frequency response matches Milgram's data (sort of: magnitude figure shows correct values but many order of magnitude off)
- Phase response is pretty close to Milgram's.





Future Work

- Investigate scaling issue with magnitude.
- Simulink model to simulate Milgram's test data.
- Rework the problem as a standard wave-maker problem and modify Howard Wilson's MatLab visualization code for a harmonically driven oscillating string.
- Further modify the code for the active wave-absorber problem.
- Implement differential flatness control on the wave-maker boundary condition. Use code to intuitive visualization